## Circle (Q 1, Paper 2)

2008

1 (a) A circle with centre $(-3,2)$ passes through the point $(1,3)$.
Find the equation of the circle.
(b) (i) Prove that the equation of the tangent to the circle $x^{2}+y^{2}=r^{2}$ at the point $\left(x_{1}, y_{1}\right)$ is $x x_{1}+y y_{1}=r^{2}$.
(ii) A tangent is drawn to the circle $x^{2}+y^{2}=13$ at the point $(2,3)$. This tangent crosses the $x$-axis at $(k, 0)$. Find the value of $k$.
(c) A circle passes through the points $a(8,5)$ and $b(9,-2)$.

The centre of the circle lies on the line $2 x-3 y-7=0$.
(i) Find the equation of the circle.
(ii) $p$ is a point on the major arc $a b$ of the circle. Show that $|\angle a p b|=45^{\circ}$.


## Answers

1 (a) $(x+3)^{2}+(y-2)^{2}=17$
(b) (ii) $k=\frac{13}{2}$
(c) (i) $x^{2}+y^{2}-10 x-2 y+1=0$

