## Linear Programming (Q 11, Paper 2)

## 2011

11. (a) The diagram shows the lines
l: $2 x+3 y-6=0$, $h: x-3=0$ and $k: y-2=0$.
Write down the three inequalities that together define the shaded region in the diagram.

(b) A garage is starting a van rental business. The garage will rent out two types of vans, small vans and large vans.

To set up the business, each small van costs $€ 20000$ and each large van costs $€ 40000$. The garage has at most $€ 800000$ to purchase the vans.

Each small van requires $18 \mathrm{~m}^{2}$ of parking space and each large van requires $24 \mathrm{~m}^{2}$ of parking space. The garage has at most $576 \mathrm{~m}^{2}$ of parking space available for the vans.
(i) Taking $x$ as the number of small vans and $y$ as the number of large vans, write down two inequalities in $x$ and $y$ and illustrate these on graph paper.
(ii) The garage charges $€ 40$ a day to rent a small van and $€ 50$ a day to rent a large van. How many of each should the garage rent to maximise rental income, assuming that all vans are rented.
(iii) The garage incurs daily expenses of $€ 12$ for each van. Calculate the maximum daily profit from renting the vans.

## Answers

11 (a) $x \leq 3, y \leq 2,2 x+3 y-6 \geq 0$
(b) (i) $x+2 y \leq 40,3 x+4 y \leq 96$
(ii) 32 small vans
(iii) $€ 896$

