## Linear Programming (Q 11, Paper 2)

2005
11 (a) The line $K$ cuts the $x$-axis at $(4,0)$ and the $y$-axis at $(0,8)$.
(i) Find the equation of $K$.
(ii) Write down the three inequalities that together define the region enclosed by $K$, the $x$-axis and the $y$-axis.

(b) A manufacturer of garden furniture produces plastic chairs and tables. Each chair requires 2 kg of raw material and each table requires 5 kg of raw material. In any working period the raw material used cannot exceed 800 kg .

Each chair requires 4 minutes of machine time and each table requires 4 minutes of machine time. The total machine time available in any working period is 1000 minutes.
(i) Taking $x$ as the number of chairs and $y$ as the number of tables, write down two inequalities in $x$ and $y$ and illustrate these on graph paper.
(ii) The manufacturer sells each chair for $€ 20$ and each table for $€ 40$.

How many of each should be produced in each working period to maximise income?
(iii) The manufacturer’s costs for each chair are $€ 17$ and for each table are $€ 34.70$. Express the profit as a percentage of income, assuming the income has been maximised.

## Answers

11 (a) (i) $2 x+y-8=0$
(ii) $x \geq 0, y \geq 0,2 x+y-8 \leq 0$
(b) (i) $2 x+5 y \leq 800, x+y \leq 250$
(ii) $x=150, y=100$
(iii) $14 \%$

