LINEAR PROGRAMMING (Q 11, PAPER 2)

1996

11 (a) The equation of the line K is y - x = 0and the equation of the line *N* is y - 4 = 0. (i) Write down the three inequalities which define the triangular region indicated in the diagram. (ii) In a diagram, illustrate the set of points (x, y) that satisfy $y - 4 \ge 0$, $y - x \le 0$ and $x-6 \le 0$. (b) A property developer wishes to construct a business centre consisting of shops and offices. The floor space required for each shop is 60 m^2 and for each office is 20 m^2 . The total floor space for the business centre cannot exceed 960 m². The construction of each shop takes 5 working days to complete and each office 3 working days to complete. The developer has at most 120 working days to complete the construction. (i) If the developer constructs x shops and y offices, write two inequalities in x and y and illustrate these on graph paper. (ii) If the rental charge is IR \pounds 200 per m² for a shop and IR \pounds 140 per m² for an office, how many of each type should be built so as to maximize the developer's rental income? Find this maximum rental income. (iii) If each shop provides 7 jobs and each office 3 jobs, write an expression in x and y for the total number of jobs to be provided. How many of each type should be built so as to maximize the number of jobs?

Answers 11 (a) (i) $y - x \ge 0$, $y - 4 \le 0$, $x \ge 0$ (b) (i) $3x + y \le 48$, $5x + 3y \le 120$ (ii) x = 0, y = 40; £5600 (iii) x = 0, y = 40