

COMPLEX NUMBERS (Q 4, PAPER 1)

2001

4 (a) Let $w = 3 - 2i$ where $i^2 = -1$.

Plot

(i) w

(ii) iw

on an Argand diagram.

(b) Solve

$$(x + 2yi)(1 - i) = 7 + 5i$$

for real x and for real y .

(c) Let $z_1 = 3 + 4i$ and $z_2 = 12 - 5i$.

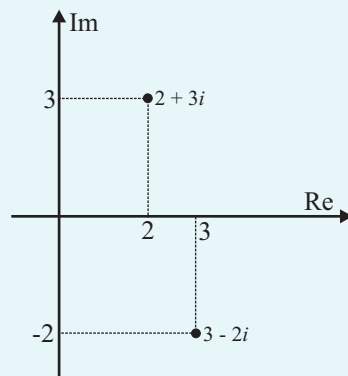
\bar{z}_1 and \bar{z}_2 are the complex conjugates of z_1 and z_2 , respectively.

(i) Show that $z_1\bar{z}_2 + \bar{z}_1z_2$ is a real number.

(ii) Investigate if $|z_1| + |z_2| = |z_1 + z_2|$.

ANSWERS

4 (a)



(b) $x = 1, y = 3$

(c) (i) 32

(ii) No