

THE CIRCLE (Q 3, PAPER 2)

2011

3. (a) A circle has equation $x^2 + y^2 = 81$.

(i) Write down the co-ordinates of the centre of the circle.

(ii) Find the radius of the circle.

(b) The circle c has equation $(x - 3)^2 + (y + 1)^2 = 17$.

(i) Verify that the point $(7, -2)$ is on c .

(ii) On a co-ordinate diagram, mark the centre of c and draw c .

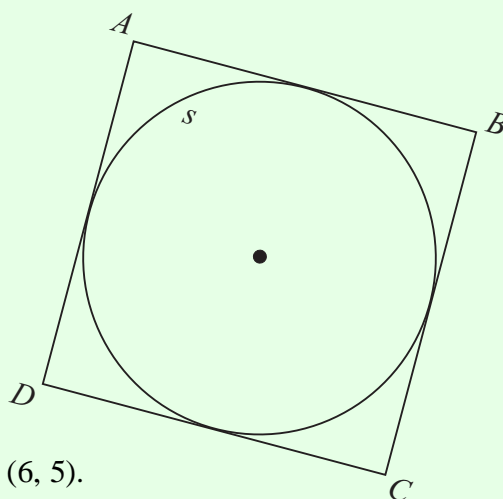
(iii) Find, using algebra, the co-ordinates of the two points at which c intersects the x -axis.

(c) The points $A(-1, 2)$, $B(-3, -4)$, $C(3, -6)$ and $D(5, 0)$ are the vertices of a square. The sides of the square are tangents to the circle s , as shown.

(i) Find the co-ordinates of the centre of s .

(ii) Find the equation of s .

(iii) The circle $(x + 4)^2 + y^2 = 10$ is the image of s under the translation $(p, q) \rightarrow (6, 5)$. Find the value of p and the value of q .



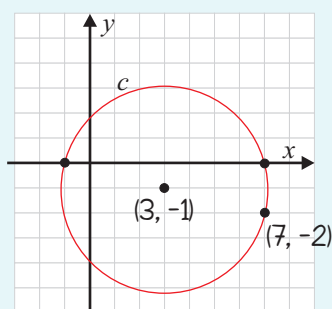
ANSWERS

3 (a) (i) $(0, 0)$

(ii) 9

(b) (ii)

(iii) $(7, 0)$, $(-1, 0)$



(c) (i) $(1, -2)$

(ii) $(x - 1)^2 + (y + 2)^2 = 10$ (iii) $p = 11$, $q = 3$